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## **HERPOR 3 – A MACROECONOMETRIC MODEL FOR THE PORTUGUESE ECONOMY**

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## **TECHNICAL SPECIFICATIONS**

**Title:** HERPOR 3 – A Macroeconometric Model for the Portuguese Economy

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## HERPOR 3 – A MACROECONOMETRIC MODEL FOR THE PORTUGUESE ECONOMY

### ABSTRACT

HERPOR is a four-sector annual macroeconomic model for the Portuguese economy, designed for policy evaluation. Although inspired in the HERMIN model, HERPOR presents several differences in relation to it, implying different results in terms of the evaluation of the impact of structural policies on the Portuguese economy.

HERPOR considers four sectors of activity: Tradable, Non-tradable, Agriculture and Non-Market services. In the short term output is mainly determined by demand and there is a trade-off between inflation and unemployment. In the long term, supply side conditions, driven by the accumulation of physical and human capital, play a key role, with actual output converging to potential output.

This paper presents a description of the third version of the model, developed in 2008, and its application to the analysis of comparative effects of different types of public expenditure shocks (Investment in infrastructures, incentives to private investment and investment in human capital).

**Keywords:** Macroeconomic model; Portugal; policy evaluation.



## HERPOR 3 – A MACROECONOMETRIC MODEL FOR THE PORTUGUESE ECONOMY

### 1. INTRODUCTION

HERPOR is a macroeconometric model for the Portuguese economy developed in the Department of Prospective and Planning (DPP) with the purpose of evaluating the macroeconomic impact of structural policies on the Portuguese economy. The model was built with the aim of considering both supply and demand side effects of these policies in the short, medium and long term.

The first version of HERPOR (described in Dias *et al.*, 2003) was completed in 2003 by a team including DPP staff and two professors from the Technical University of Lisbon (ISEG). This version was used in the mid-term evaluation of the Community Support Framework 2000-2006, CSF III (Dias *et al.*, 2003) and in the evaluation of the Portuguese Central Government Investment Programme, PIDDAC (Dias and Lopes, 2004).

Lopes (2005) developed in his Master's thesis an adapted version of HERPOR to simulate the impact (on the Portuguese economy and on Social Security financing) of alternative changes in the Social Security system for Portugal (*vide* also: Garcia and Lopes, 2006).

In 2005 the model was revised and updated in order to be used in the update of CSF III mid-term evaluation, originating the second version of HERPOR, presented in Dias and Lopes (2005) and in Dias (2006). This version was also used in the *ex-ante* evaluation of the National Strategic Reference Framework 2007-2013 (NSRF), presented in Dias and Lopes (2007a) and in Dias (2007).

In 2008 the model data basis was totally revised and updated in order to make it compatible with basis 2000 of National Accounts. This revision implied the complete reestimation, and in some cases, re-specification, of the model, giving birth to HERPOR 3, which is the object of the present paper.

The next section presents a model description, starting with general features, followed by an explanation of the demand and supply mechanisms (in the short and in the long-run) present in the model and completed with the description of the public finance block.

Section 3 refers to model estimation and validation, including the presentation of model historical simulation results. Section 4 presents model applications, including

the comparative analysis of the effect of the main three types of public expenditure co-financed by European structural funds (investment in infrastructures, incentives to private investment and investment in human capital).

Appendixes 1 to 6 complete this paper, presenting details of model specification, estimation and simulation.

## 2. MODEL DESCRIPTION

### 2.1. General features

HERPOR was initially inspired in the HERMIN model<sup>1</sup>, in its version for Portugal. The HERMIN modelling framework was designed in the 1990s to evaluate the economic impact of EC structural interventions in Objective 1 countries (Bradley *et al.*, 1995; Bradley, 2000; Bradley and Untiedt, 2007).

Although inspired in HERMIN, HERPOR differs from it in many aspects of model specification, methods of parameter estimation and in the data basis used for estimation, implying different results in terms of the evaluation of the impact of structural policies on the Portuguese economy<sup>2</sup>.

The main features of HERPOR model are:

- The sectoral breakdown in four sectors: A (Agriculture, Forestry and Fishing), T (tradable sector, including Mining, Manufacturing and Air and Water Transportation Services), N (non-tradable market sector, including Building and Construction, Utilities and other market services) and G (predominantly non-market services: Public Administration, Education, Health and Social services and Sanitation)<sup>3</sup>;
- The essentially exogenous nature of the A and G sectors;
- In the short term, output in the T and N sectors is mainly determined by demand;
- The existence of a short-term trade-off between wage growth and unemployment;
- The leading role of the Tradable sector in wage determination;

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<sup>1</sup> We are grateful to Professor John Bradley (the main author of HERMIN models) for his willingness to discuss all the features of HERMIN with the HERPOR team as well as for providing us all the information and files concerning various versions of HERMIN Portugal, and for his valuable comments on HERPOR's second version.

<sup>2</sup> A comparison of results of the impact of CSF III on the Portuguese economy, evaluated with HERPOR (version 2) vs. HERMIN and QUEST II, is presented in Dias (2006), pp 14-16.

<sup>3</sup> A complete identification of HERPOR sectors is presented in Appendix 4.



- Exports and imports are not explicitly modelled and the trade balance is obtained through the difference between GDP and total domestic demand;
- The consideration of long-term (supply-side) effects of public policies promoting changes in physical and human capital stocks;
- Parameters of behavioural equations mostly obtained from econometric estimation, considering long-run (cointegrating) and short-run relationships (with an error-correction mechanism);
- Explicit modelling of potential output as a function of productive factors (stock of infrastructures, stock of productive capital, human capital and labour).

HERPOR specification was also influenced by other modelling experiences of the HERPOR team, such as MEGA (Dias and Lopes, 2007b), a macroeconometric model also developed in DPP, which influenced the modelling of the Public Finance block and of Private Consumption in HERPOR.

## 2.2. Output, Demand and Balance of Goods and Services

GDP (at basic prices) is obtained through the sum of sectoral **output** (gross value added) across the four sectors.

Output in the **T** and **N** sectors depend on both domestic and international demand and, in the case of the T sector, also on profitability (proxied by real unit labour costs) and on price competitiveness (ratio of internal to international manufacturing prices). The relevance of international demand for explaining output in the N sector results from the fact that this sector has an increasing tradable component, particularly through tourism and, more recently, through the internet.

Real output in the **A** sector is exogenous.

In the **G** sector, given the predominance of Public Administration, nominal output is defined as the sum of a set of exogenous components (compensation of employees, self-employed income and other). Real output is obtained through the ratio between nominal output and its deflator.

Real **private consumption** depends on real personal disposable income and also on the unemployment and interest rates.

Real **public consumption** is obtained from the ratio of nominal public consumption (exogenous) to an endogenous public consumption deflator.

Total fixed **investment** is obtained through the sum of sectoral investment across all sectors to housing investment.

Real investment in Agriculture and nominal investment in infrastructures (defined as the sum of the investment in sector G with infrastructural investment in sector N<sup>4</sup>) are exogenous.

Investment in the N sector (excluding housing and infrastructures) depends positively on sectoral output and negatively on real interest rate, unemployment rate and the relative price of investment goods. It is also assumed that public incentives to this investment have a positive additive effect on it. Therefore, this aid was included as an explanatory variable.

Investment in the tradable sector depends positively on sectoral output and output gap and negatively on the user cost of capital. For this sector the econometric tests did not allow the acceptance of an additive effect of public aid on investment. In this case public aid has only an indirect effect on investment through the lowering of the user cost of capital.

Housing investment depends positively on real household disposable income and negatively on nominal interest rates and on a dummy assuming value 1 from 2003 onwards (reflecting legislation revision, occurred in 2002, which ended interest rate bonuses to housing loans).

**Domestic demand** addressed to sectors N and T is calculated through weighted sums of domestic demand components (private consumption, public consumption, investment in construction and investment in equipment), using coefficients derived from input-output matrices estimated for 2005 (Dias, 2008 and 2009). These coefficients represent the estimated value added content (direct+indirect) concerning the T and N sectors respectively, per unit of each domestic demand component<sup>5</sup>.

The **Balance of Goods and Services** is obtained through the difference between GDP at market prices and total domestic demand.

### 2.3. Long-Term Supply and Potential Output

Long-term supply is determined by potential output, calculated through **production functions**. Production function modelling in HERPOR is inspired in Pina and St. Aubyn (2002), using Cobb-Douglas functions with four productive factors: labour (employment in volume), human capital (measured by the average number

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<sup>4</sup> Infrastructural Investment in sector N was defined as the investment in construction in the branches of water, electricity, gas, land and pipeline transport, supporting transport activities and communications.

<sup>5</sup> The methodology for calculating value added contents of final demand is explained in Dias (2010).

of years of training in the working age population), public capital (or capital of infrastructures) and private capital (excluding housing). Constant returns to scale are assumed in labour and fixed capital.

In HERPOR two production functions are considered: one for the whole economy and another for the T sector.

Given the existence of problems of multicollinearity not all the production function parameters were econometrically estimated and some of them were calculated on the basis of theory-based and empirical assumptions.

In the **aggregate production function** the elasticities of (potential) GDP in relation to public and private fixed capital and to labour were calculated on the basis of the following assumptions: (i) constant returns to scale regarding these three productive factors; (ii) a 5% average real rate of return on both public and private capital. The elasticity of GDP in relation to human capital was then econometrically estimated, but we could not accept the constancy of this elasticity over time and so we estimated a time varying elasticity, which decreases over time (from 1.29 in 1977 to 1.01 in 2006).

For the **Tradable sector** we also assumed constant returns to scale in labour and fixed capital and a 5% average real rate of return on private capital but no assumption was made regarding public capital and so we estimated freely the parameters for public capital and for human capital. However we did not obtain an economically acceptable elasticity for public capital (the estimated parameter was negative) so we excluded public capital from the tradable sector production function. In this case we accepted a constant elasticity of output regarding human capital of 0.78.

**Stocks of fixed capital** are calculated from investment flows (decomposed into investment in equipment and investment in construction, with different depreciation rates) using the perpetual inventory method.

The **stock of human capital** (defined as the average number of years of schooling and training for population aged 15 to 64) is obtained through the sum of the stocks of academic education and of professional training. For simplification, the first is exogenous and the second is a function of investment in training. For the stock of academic education we used an updated version of the series estimated by Pereira (2003), concerning the average number of years of schooling of the working age population. The stock of professional training was estimated in DPP on the basis of the results of surveys made by the Ministry of Labour (DETEFP, 2000-2006) and of data concerning expenditure on professional training co-financed by EU structural funds (CSF and NSRF).

The production functions included in the model allow the estimation of potential output and **output gaps** for the whole economy and for the tradable sector. These output gaps interact with the other variables in the model, influencing labour demand and investment.

#### 2.4. Short-Term Supply mechanisms: Labour Market, Wages and Prices

The labour market modelling plays an important role in the model self-stabilization properties, understood as the mechanisms that ensure convergence for a long-term equilibrium guided by supply conditions.

**Labour demand** (Employment) in the T and N sectors depends negatively on the real cost of labour and positively on sectoral output and on output gaps (in the T sector and in the whole economy, respectively). The latest link contributes to the closure of output gaps: In fact, a positive gap imply an increase in employment, pushing up potential output on one hand and making pressure on wages and prices (associated to the reduction of the rate of unemployment), which contributes to a loss in competitiveness, reducing total demand and actual output.

Agricultural employment is exogenous. In the G sector employment is obtained through the division of total compensation of employees (exogenous) by an endogenous wage rate.

**Labour supply** is a function of employment opportunities. This equation assumes an open policy in relation to migration flows in order to allow an adjustment between supply and demand in the labour market.

The Tradable sector assumes a leading role in **wage** determination for the whole economy. The wage rate equation for this sector is specified in such a way so that the change in the labour share depends negatively on the rate of unemployment. There is an implicit equilibrium rate of unemployment corresponding to the stabilisation of the labour share, which is 5.9%, according to the estimated parameters. This value is close to some NAIRU estimates for the Portuguese economy such as in Martins and St.Aubyn (2001).

The wage rate growth in the various sectors (including the G sector) is guided by the Tradable sector, following the logic of the so-called Scandinavian model.

In the N sector the wage rate growth is also influenced by the productivity growth differential in relation to the T sector.

In sector G the wage rate growth depends also on the unemployment rate and on the public deficit (in percentage of GDP) observed in the previous period.

Internal **prices** are influenced by unit labour costs and by international prices.

Deflators of sectoral value added play a key role in the whole model price determination. Deflators for the T and N sectors depend on unit labour costs and on international prices converted to euros. Sector A has an exogenous deflator and the deflator for sector G is related to the corresponding gross wage rate (including employer's contributions).

GDP deflator at basic prices (PGDPBP) results from a weighted average of sectoral value added deflators. GDP deflator at market prices (PGDPM) is determined by PGDPBP and by the tax rate on products (net of subsidies).

Deflator of private consumption depends on PGDPM and on import prices (exogenous).

The deflator of investment in equipment depends on import prices and on the OT deflator.

The deflator of investment in construction depends on import prices and on labour costs in sector N (which includes the construction sector).

Finally, public consumption deflator depends on the deflator of value added in sector G.

## **2.5. Public Finance**

Taxes and social contributions are functions of the corresponding tax basis (or a proxy of it) multiplied by exogenous tax rates: direct taxes on households (depending on personal income before tax) and on companies (depending on Profits), social contributions (depending on total wage bill), indirect taxes (depending on private consumption) and capital taxes (depending on GDP). Public sector investment income is also a function of GDP.

On the expenditure side, public consumption is obtained through the sum of two exogenous components (compensation of employees in the G sector and other public consumption expenditure). Public transfers, subsidies and public investment are also exogenous. Interest payments depend on the level of public debt multiplied by an exogenous interest rate.

Public deficit, obtained from the difference between total expenditure and total revenue, determines the evolution of public debt.

The above description corresponds to the standard version of the model, used in reference simulations. For variant simulations (used to evaluate the impact of policies and other exogenous shocks), a fiscal policy rule is often included in order to equate the public deficit (as percentage of GDP) to the reference scenario. This

rule is particularly important in the evaluation of policies involving additional public expenditure because it ensures its financing.

In the fiscal policy rule version, public deficit as a percentage of GDP is an exogenous variable (equal to the value simulated in the reference scenario) and the adjustment is made through the rate of taxation (less subsidies) on products.

### **3. MODEL ESTIMATION AND VALIDATION**

For the model estimation a data basis was built with annual data from, at least, 1977 to 2006 (1958 to 2006, when possible), making series from different accounting systems compatible with basis 2000 of National Accounts.

HERPOR 3 has 142 equations of which 20 were econometrically estimated, two had their parameters calculated from input-output matrices and the remaining 120 are identities, definition or calibrated equations.

The estimated equations concern actual output (value added) for the T and N sectors, potential output (production functions – for the whole economy and for the T sector), investment (for the T and N sectors and for housing), wage rates in the four sectors, prices in the T and N sectors, deflators for consumption, equipment and construction, employment in the T and N sectors, private consumption and labour force.

Details of equation estimation are presented in Appendix 2. In principle the largest possible estimation period was used given the available actual data, unless there was evidence of structural change along that period.

Given the fact that a large number of the model series are non stationary (mostly I(1) in the logs), the econometric estimation was done considering, for most of the equations, long-run cointegration relationships and short-run relationships with an error-correction mechanism (ECM). These relationships were estimated either in two steps (following the procedure proposed by Engle and Granger, 1987) or in one step, using, in both cases, Ordinary Least Squares (OLS) or, for some cases of imposed parameter restrictions, Restricted Least Squares (RLS).

For each variable, several regressions were attempted with specifications inspired in economic theory and in the perceived behaviour of the Portuguese economy. Estimated equations were, in principle, only accepted when the estimated coefficients were statistically significant<sup>6</sup> and presented economically acceptable

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<sup>6</sup> In some cases “non-significant” variables were kept in some equations for theoretical reasons or because their inclusion improved the overall performance of the model.

signs and values, the regression was globally significant and the residuals of the regression were “well behaved” (stationary in the case of long-run relationships, a condition for accepting cointegration; white-noises in the case of short-run relationships).

After the “best” regression equation was selected for each variable, the model was simulated as a whole in the sample period and in a projection period but initially the results were not satisfactory and so many alternative model versions were tried, with different equation combinations, before an acceptable model version was found.

Therefore, the criteria for equation selection was not only the goodness of fit of each regression itself but also the global performance of the model in the historical simulation and in the long-run projections and so, for some variables, the equations finally included in the model were not the best regressions assessed by individual equation criteria.

The inclusion of some parameter restrictions, such as a long-term unit income elasticity of private consumption, proved to be useful for the long-run model behaviour.

The 2008 model revision used the 2005 specification as a starting point for model reestimation with updated data and specification changes were introduced only when individual equation results or global model simulation were not satisfactory.

Particular attention was given to the equation performance in the most recent years of the sample period since a poor fit in this period might evidence recent structural changes which would disable the model for simulations in the future (one important purpose of the model).

The results of historical dynamic simulation of the whole model, for key economic variables, in 1981-2006, are presented in table 1 and in Appendix 5 (graphs).

Besides minimising simulation errors for the key variables, one concern for model selection was that it succeeded in simulating correctly the turning points observed in the Portuguese economy, which was basically achieved as it can be confirmed from the graphs for GDP in Appendix 5.

In addition to a good replication of the past it was also important to ensure that the model was well behaved in the long-run, producing acceptable reference scenarios for the future and responding to economic shocks in compliance with economic theory and empirical observation. This was confirmed through model simulations until 2050 (reference scenario and simulation of shocks).

**Table 1 – Historical dynamic simulation (1981-2006) of HERPOR (version of 2008)**

**Simulation errors (%):**

| Variable | Description                       | RMSPE | MAPE | MPE  |
|----------|-----------------------------------|-------|------|------|
| GDPM     | real GDP at market prices         | 2,4   | 1,8  | -0,6 |
| OT       | real Gross Value Added - T sector | 3,6   | 3,2  | -0,7 |
| ON       | real Gross Value Added - N sector | 2,5   | 1,9  | -0,5 |
| CONS     | real Private Consumption          | 2,4   | 1,8  | -0,4 |
| I        | real Fixed Investment             | 4,1   | 3,1  | -0,4 |
| PGDPM    | GDP deflator                      | 3,4   | 2,2  | 0,5  |
| LF       | Labour Force                      | 1,2   | 1,0  | -0,3 |
| L        | Total Employment                  | 1,9   | 1,6  | -0,4 |
| W        | Wage rate                         | 4,9   | 3,9  | 0,8  |

**Simulation errors (percentage points):**

| Variable    | Description                        | RMSE | MAE | ME  |
|-------------|------------------------------------|------|-----|-----|
| UR          | Unemployment rate                  | 0,9  | 0,8 | 0,2 |
| NTSV/GDPMV% | Bal. Goods and Services (% of GDP) | 1,2  | 0,9 | 0,2 |
| GBORR       | Public deficit (% of GDP)          | 0,8  | 0,7 | 0,0 |

$$\text{RMSPE (Root Mean Square Percent Error)} = \left( \frac{\sum_{t=1}^N [(Y_{S_t} - Y_{A_t})/Y_{A_t}]^2}{N} \right)^{0.5} * 100$$

$$\text{MAPE (Mean Absolute Percent Error)} = \left\{ \frac{\sum_{t=1}^N |(Y_{S_t} - Y_{A_t})/Y_{A_t}|}{N} \right\} * 100$$

$$\text{MPE (Mean Percent Error)} = \left[ \frac{\sum_{t=1}^N [(Y_{S_t} - Y_{A_t})/Y_{A_t}]}{N} \right] * 100$$

$$\text{RMSE (Root Mean Square Error)} = \left[ \frac{\sum_{t=1}^N (Y_{S_t} - Y_{A_t})^2}{N} \right]^{0.5} * 100$$

$$\text{MAE (Mean Absolute Error)} = \left( \frac{\sum_{t=1}^N |Y_{S_t} - Y_{A_t}|}{N} \right) * 100$$

$$\text{ME (Mean Error)} = \left[ \frac{\sum_{t=1}^N (Y_{S_t} - Y_{A_t})}{N} \right] * 100$$

where  $Y_S$  and  $Y_A$  are the simulated and actual values of an endogenous variable and  $N$  is the number of simulation periods (26 in this case).

## 4. MODEL APPLICATIONS

### 4.1. Evaluation of the impact of structural policies

HERPOR has been used in the evaluation of the impact of exogenous shocks, in particular shocks of public expenditure co-financed by European Union structural funds.

Each evaluation is made through the comparison of the results of two model simulations, performed for a long period (*eg.* until 2050), to allow the evaluation of long-term effects:

- a reference simulation, reproducing the observed/projected path for the Portuguese economy;
- a simulation corresponding to what would happen to the economy in the absence (presence) of the shock subject to evaluation (depending on whether the shock is already included or not in the reference simulation). This simulation is performed after revising the values of the exogenous variables in order to exclude (include) the direct effect of the shock on them.



The macroeconomic impact of the shock is usually measured through the percent deviation between the two simulations for each model variable

Portugal has benefited from community structural funds, since it joined the European Community in 1986, with the purpose of stimulating real convergence of the Portuguese economy to the average European levels. Since 1989 this community support was framed by the Community Support Frameworks (CSF: CSF I, from 1989 to 1993; CSF II, from 1994 to 1999; CSF III, from 2000 to 2006) and, more recently, by the National Strategic Reference Framework 2007-2013 (NSRF).

The second version of HERPOR was used for the interim evaluation of CSF III (which included also the evaluation of the impact of CSF I+II+III) and the *ex-ante* evaluation of NSRF. The results of these exercises are presented in Dias and Lopes (2005 and 2007a), for CSF and NSRF, respectively, as well as in Dias (2006), for CSF and in Dias (2007), for both CSF and NSRF.

HERPOR 3 is currently being used for an interim evaluation of the macroeconomic impact of the NSRF, considering the expenditure already made for the period 2007-2009 and the projected expenditure for 2010-2015.

The intensity of CSF/NSRF impact on the economy depends on the level of the corresponding implemented expenditure<sup>7</sup> as well as on its structure. Three main types of expenditure are considered in the evaluation: Investment in infrastructures, incentives to private investment and investment in human capital.

#### **4.2. Comparing the impact of different types of public expenditure**

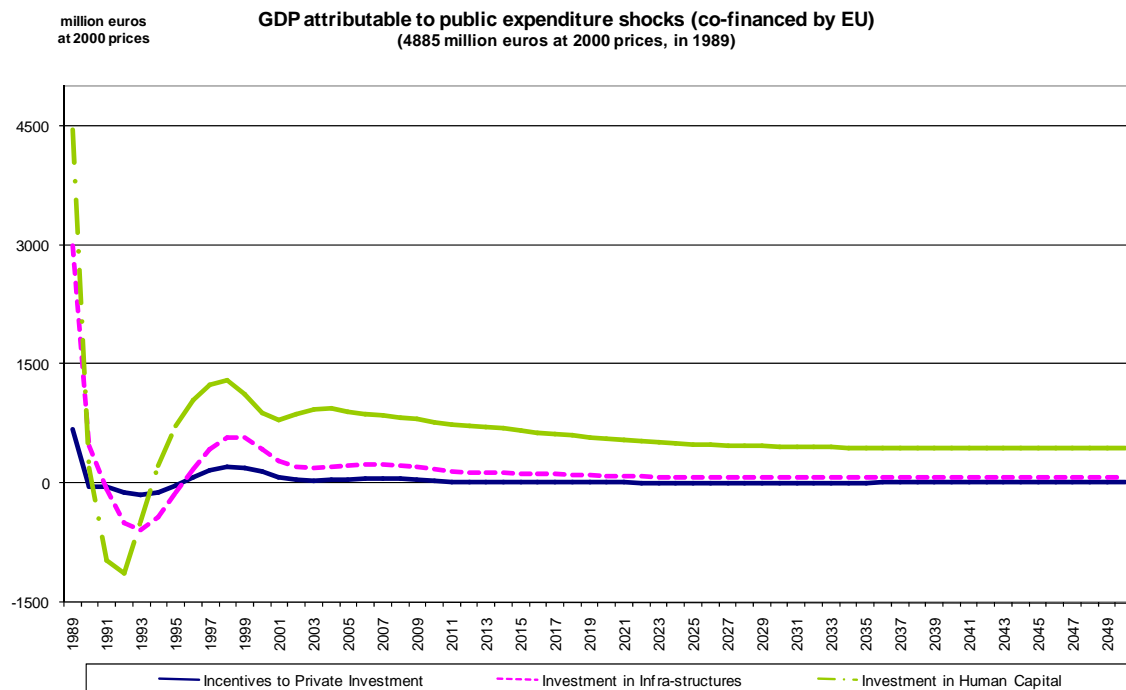
In order to compare the effect of different types of expenditure co-financed by EU structural funds, we applied public expenditure shocks of 2500 million euros in 1989 (equivalent to 4885 million euros at 2000 prices), co-financed by EU funds at rates similar to those observed for CSF, and performed model simulations (with the fiscal policy rule option) for the period 1989-2050, for each of the main types of expenditure. The results of this exercise are presented in Graphs 1 and 2 (and Appendix 6) which show the impacts of the three main types of CSF/NSRF expenditure (investment in infra-structures, incentives to private investment<sup>8</sup> and investment in human capital).

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<sup>7</sup> Only public expenditure was considered in the evaluations, assuming that the private component of CSF/NSRF expenditure would be spent with or without CSF/NSRF, although with different applications.

<sup>8</sup> The impact of incentives to private investment depends on the sector of activity to which it is applied. The results presented in this paper are based on a sectoral breakdown of incentives similar to the average observed for the three CSF.

**Graph 1**



The cumulated impact on GDP per euro of public expenditure was calculated<sup>9</sup> for each type of expenditure and it is presented in Graph 2.

As it is evidenced by the graphs, Investment in Human Capital is the type of expenditure that presents the greater impact on GDP per euro invested<sup>10</sup> (in the short-term as well as in the long-term), followed by Investment in Infra-structures. Incentives to Private Investment present the lowest effect with an additional long-run cumulated GDP per euro invested, estimated in 0.3 euros, which compare with 1.3 euros for infra-structures and 4 euros for Human Capital.

In all cases there are temporary negative effects in the medium-term, normally between the third and fifth or sixth year after the application of the shock (execution of public expenditure) which result from the inflationary temporary effect of demand pressure. The relationship between demand and supply is

<sup>9</sup> The formula of calculation for this indicator ( $Z_t$ ) is (all values at constant prices):

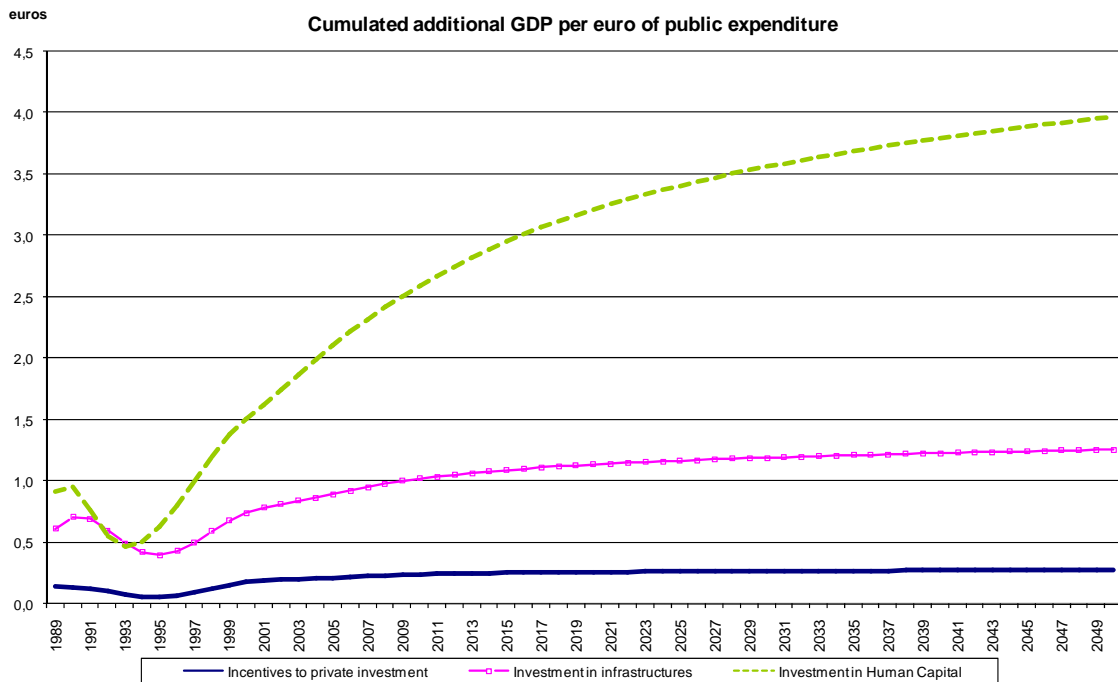
$$Z_t = \frac{\sum_{k=0}^t [Y_k / (1+i)^k]}{D} \quad \text{where } Y_k \text{ is GDP attributable to the expenditure shock, generated in year } k$$

(difference between the values for the scenarios “with” and “without” the shock),  $D$  is the value of the expenditure shock and  $i$  is a discount rate (3%), to account for inter-temporal preference.  $k=0$  represents the year of the expenditure shock (1989). The long-term value for this indicator (for  $t=\infty$ ) may be interpreted as a Benefit-to-Cost ratio for the expenditure shock (assuming that the benefits are measured by additional GDP) or as a total long-run (discounted) multiplier of GDP in relation to this public expenditure, a value above 1 representing a real rate of return above the discount rate (and vice-versa).

<sup>10</sup> Note that, as the model is non-linear, multiplier effects may vary according to the size and time of the shock.

illustrated by graphs A6-3 to A6-5, in Appendix 6, where the effects on actual and potential output are compared.

**Graph 2**



The greater impact of Investment in Human Capital in the short-run, compared to the other types of expenditure, results from its lower import content as it implies directly an increase in the output of sector G (corresponding to the production of education and training services) and, indirectly, an increase in the output of sectors T and N to satisfy domestic demand boosted by the higher household disposable income associated to both scholarships and payments to instructors. The short-term impact of the Investment in Infra-structures is slightly lower due to its higher import content in equipment and materials. In relation to the Incentives to Private Investment, its short-term effect is even lower than that of infra-structures not only because private investment has an import content higher than investment in infra-structures but also because, in the case of the Tradable sector, these incentives have only, according to the estimated model, an indirect effect on investment (through the reduction of the user cost of capital) implying a relatively low impact on that investment.

In the long-run, the greater impact of investment in human capital compared to the other types of expenditure results also from the estimated parameters for the global production function which imply a higher direct effect on potential output of one euro of investment in human capital, compared to investment in infra-structures or in private investment. Graph A6-1 (Appendix 6) presents the impact of different types of expenditure on potential output.

The impact of different types of expenditure on Employment is illustrated by graph A6-2. After a positive initial impact, the effect on employment becomes negative in the medium term and virtually zero in the long-term in the case of investment in infra-structures and of incentives to private investment. In relation to investment in human capital the negative impact on Employment is more intense and it lasts for the long-term due to high impact of this type of expenditure on labour productivity, which is stronger than the impact on total output.

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## APPENDIX 1 – HERPOR 3 – a simplified presentation

|   | Sectors of activity                                      |  |  |  | Global economy  |
|---|--|--|--|--|---|
|   | T  | N  | A                                      | G                                      |   |
| <b>1. Output and Demand at 2000 prices:</b>     |  |  |  |  |   |
| Actual output                                   | $OT = f(FDOT, OW, POT/PWORLD, ULCT/POT, T)$              | $ON = f(FDON, OW)$                                       | OA EXOGENOUS                           | OG = OGV / POG                         | GDPBP = OT + ON + OA + OG                                 |
| Potential output                                | $OTPOT = f(KT, KTRAIN, LT)$                              |  |  |  | $YPOT = f(KPR, KINF, KTRAIN, T, L)$                       |
| Output gap                                      | $GAPOT = \log(OT) - \log(OTPOT)$                         |  |  |  | $GAPGDP = \log(GDPBP) - \log(YPOT)$                       |
| GDP at market prices                            |  |  |  |  | GDPM = GDPBP + TP / PTP                                   |
| Domestic demand                                 | $FDOT = 0.06 * CONS + 0.02 * G + 0.10 * IC + 0.07 * IME$ | $FDON = 0.46 * CONS + 0.13 * G + 0.59 * IC + 0.31 * IME$ |  |  | DD = CONS + G + I + DS                                    |
| Private Consumption                             |  |  |  |  | $CONS = f(YRPERD, IRD, UR, T)$                            |
| Public Consumption                              |  |  |  |  | G = GV / PG   |
| Total Fixed Investment (GFCF)                   |  |  |  |  | I = IT + IN + IA + IG + IH                                |
| Fixed Investment excl.housing                   | $IT = f(OT, PKT, CSFT, GAPOT)$                           | IN = IN2 + ININF   | IA EXOGENOUS                           | IG = IGV / PIG                         |   |
| Inv.excl.Infrastr. and Housing                  |  | $IN2 = f(ON, UR, PIN2/PON, RIRLT, TRIN/PIN2)$            |  |  |   |
| Inv. in Equipment                               | $ITME = WITME * IT$                                      | $INME = WIN2ME * IN2$                                    | $IAME = WIAME * IA$                    | $IGME = WIGME * IG$                    | IME = IAME + ITME + INME + IGME                           |
| Inv. Construction excl.Housing                  | $ITBC = IT - ITME$                                       | $INBC = IN - INME$                                       | $IABC = IA - IAME$                     | $IGBC = IG - IGME$                     | IBC = IABC + ITBC + INBC + IGBC                           |
| Housing investment                              |  |  |  |  | $IH = f(YRPERD, IRLT, d2003ih)$                           |
| Inv. in Construction                            |  |  |  |  | IC = IBC + IH   |
| Inv. in infrastructures                         |  | $ININF = ININFV / PIC$                                   |  |  | IINF = ININF + IG   |
| Change in inventories                           |  |  |  |  | DS = ADS * (OA + OT + ON)                                 |
| Ext. Balance of Goods & Serv.                   |  |  |  |  | NTS = GDPM - DD   |
| <b>2. Physical capital stock at 1995 prices</b> |  |  |  |  |   |
| Cap.stock - Constr.excl.Hous.                   | $KTBC = (1 - DEPBC) * KTBC(-1) + ITBC$                   | $KNBC = (1 - DEPBC) * KNBC(-1) + INBC$                   | $KABC = (1 - DEPBC) * KABC(-1) + IABC$ | $KGBC = (1 - DEPBC) * KGBC(-1) + IGBC$ |   |
| Capital stock - Equip.                          | $KTME = (1 - DEPME) * KTME(-1) + ITME$                   | $KNME = (1 - DEPME) * KNME(-1) + INME$                   | $KAME = (1 - DEPME) * KAME(-1) + IAME$ | $KGME = (1 - DEPME) * KGME(-1) + IGME$ |   |
| Physical cap.stock excl.Hous.                   | $KT = KTBC + KTME$                                       | $KN = KNBC + KNME$                                       | $KA = KABC + KAME$                     | $KG = KGBC + KGME$                     |   |
| Stock of Infrastructures                        |  | $KNINF = (1 - DEPBC) * KNINF(-1) + ININF$                |  |  | $KINF = KG + KNINF$                                       |
| Phys.cap.stock excl.infr.&Hous.                 |  |  |  |  | $KPR = KA + KT + KN - KNINF$                              |
| <b>3. Human capital</b>                         |  |  |  |  |   |
| Stock of professional training                  |  |  |  |  | $KPTRAIN = KPTRAIN(-1) * (1 - DEPTRAIN) + PTRAIN / N1564$ |
| Total human capital                             |  |  |  |  | $KTRAIN = KEDU + KPTRAIN$                                 |
| <b>4. Output and Demand at current prices:</b>  |  |  |  |  |   |
| Actual output                                   | $OTV = OT * POT$   | $ONV = ON * PON$   | $OAV = OA * POA$                       | $OGV = YWG + YGSEMP + OGVO$            | GDPBPV = OTV + ONV + OAV + OGV                            |
| GDP at market prices                            |  |  |  |  | GDPMV = GDPBPV + TP                                       |
| GDP at factor costs                             |  |  |  |  | $GDPFCV = GDPMV - TI + SUB$                               |
| Private Consumption                             |  |  |  |  | CONSV = PCONS * CONS                                      |
| Public Consumption                              |  |  |  |  | $GV = YWG + GENW$   |
| Total investment                                |  |  |  |  | $IV = ITV + INV + IAV + IGV + IHV$                        |
| Total Investment excl.housing                   | $ITV = ITBC * PIC + ITME * PIME$                         | $INV = INBC * PIC + INME * PIME$                         | $IAV = IABC * PIC + IAME * PIME$       | $IGV = IS13V + IGVO$                   |   |
| Housing investment                              |  |  |  |  | $IHV = IH * PIC$  |
| Change in inventories                           |  |  |  |  | DSV = PDS * DS  |
| Ext. Balance of Goods & Serv.                   |  |  |  |  | NTSV = GDPMV - (CONSV + GV + IV + DSV)                    |

## APPENDIX 1 – HERPOR 3 – a simplified presentation (continued)

| Sectors of activity |   |   |   | Global economy |
|---------------------|---|---|---|----------------|
| T                   | N | A | G |                |

### 5. Prices and costs:

|                                    |   |                             |                |  |   |
|------------------------------------|---|-----------------------------|----------------|--|---|
| Output deflators                   | POT = f (PWORLD, ULCT)  | PON = f (ULCN, PWORLD)      | POA EXOGENOUS  | POG = POGW * WG                        | PGDPBP = GDPBPV / GDPBP                                   |
| deflator of GDP at market prices   |   |                             |                |  | PGDPM = GDPMV / GDPM                                      |
| Private Consumption deflator       |   |                             |                |  | PCONS = f (PM, PGDPM)                                     |
| Public Consumption deflator        |   |                             |                |  | PG = RPGO * POG   |
| Investment deflators               | PIT = ITV / IT  | PIN = INV / IN              | PIA = IAV / IA | PIG = WIGME * PIME + (1 - WIGME) * PIC | PI = IV / I   |
| Defl. Inv.excl.infr.and housing    |   | PIN2 = (INV - ININFV) / IN2 |                |  | PIME = f (PM, POT)  |
| Defl. Investment in Equipment      |   |                             |                |  | PIC = f (PM, WN, ULCN, T)                                 |
| Defl. investment in Construction   |   |                             |                |  | PTP = PTP(-1) * PCONS / PCONS(-1) * RTP / RTP(-1) * ADPTP |
| Defl.of Taxes-Sub. on products     |   |                             |                |  |   |
| User cost of capital               | PKT = PIT / POT * ((1 + IRLT / 100) / (PIT / PIT(-1))) * (1 + DEPT) - 1 |                             |                |  | RIRLT = (1 + IRLT / 100) / (PCONS / PCONS(-1)) - 1        |
| Real interest rate of credit       |   |                             |                |  |   |
| Depr. rate of capital stock        | DEPT = 1 - (KT - IT) / KT(-1)   |                             |                |  |   |
| Weight of inv.aid on total invest. | CSFT = TRIT / ITV   |                             |                |  |   |

### 6. Labour market, labour productivity, labour costs and profits

|                              |                              |                                |                            |                                |  |
|------------------------------|------------------------------|--------------------------------|----------------------------|--------------------------------|--|
| Total Employment             | LT = f (OT, GAPOT, WT / POT) | LLN = f (ON, GAPGDP, ULCN/PON) | LA EXOGENOUS               | LG = LGEMP + LGSEMP            | L = LA + LT + LLN + LG                       |
| Self employment              | LTSEMP = SETRA * LT / 100    | LLNSEMP = SENRAT * LN / 100    | LASEMP = SEARAT * LA / 100 | LGSEMP = YGSEMP / (1.157 * WG) | LEMP = LAEMP + LGEMP + LLNEMP + LTEMP        |
| Employees                    | LTEMP = LT - LTSEMP          | LLNEMP = LLN - LLNSEMP         | LAEMP = LA - LASEMP        | LGEMP = YWG / WG               |  |
| Labour Force                 |                              |                                |                            |                                | L F = f (L)                                  |
| Unemployment rate            |                              |                                |                            |                                | UR = 100 * ((LF - L) / LF)                   |
| Wage rate                    | WT = f (LPRT, POT, UR)       | WN = f (WT, LPRN/LPRT)         | WA = f (WT)                | WG = f (WT, GBORR, UR)         | W = YW / LEMP                                |
| Real wage rate (sectors T+N) |                              |                                |                            |                                | WR = (YWT + YWN) / (LTEMP + LLNEMP) / PGDPBP |
| Labour productivity          | LPRT = OT / LT               | LPRN = ON / LLN                |                            |                                | LPROD = GDPBP / L                            |
| Unit labour costs            | ULCT = WT / LPRT             | ULCN = WN / LPRN               |                            |                                | ULC = W / LPROD                              |
| Compensation of employees    | YWT = LTEMP * WT             | YWN = LLNEMP * WN              | YWA = LAEMP * WA           | YWG EXOGENOUS                  | YW = YWT + YWN + YWA + YWG                   |
| Profits                      | YCT = OT - YWT               | YCN = ON - YWN                 | YCA = OA - YWA             |                                | YC = GDPBPV - YW                             |



## APPENDIX 1 – HERPOR 3 – a simplified presentation (continued)

| Variable  | Model version              | Equation  |
|---|----------------------------|---|
| <b>7. Personal income</b>                         |                            |   |
| Personal income before tax                        |                            | $YPER = GDPFCV * (1 - RCS) + YFN + BTPRNE - GTYC - GTYSOC + GTR + GTRND - GTTI$                           |
| Personal disposable income                        |                            | $YPERD = YPER - GTYPER - TD2S$  |
| Real personal disposable income                   |                            | $YRPERD = YPERD / PCONS$  |
| <b>8. Public Finance</b>                          |                            |   |
| Direct taxes on households                        |                            | $GTYPER = RGTYPER * YPER$   |
| Direct taxes on corporations                      |                            | $GTYC = RGTYC * YC(-1)$   |
| Social contributions received by Publ.Adm.        |                            | $GTYSOC = RGTYSOC * YW$   |
| Taxes less Subsidies on products                  |                            | $TP = RTP * CONSV$  |
| Capital taxes                                     |                            | $GTK = RGTK * GDPMV$  |
| Public sector investment income                   |                            | $GTTI = RGTTI * GDPMV$  |
| Interest on public debt                           |                            | $GTRND = (RGDI / 100) * ((GND(-1) + GND) / 2)$  |
| Total subsidies                                   |                            | $SUB = GSUB + ECSUB$  |
| Public debt                                       |                            | $GND = GND(-1) + GBOR + DAT$  |
| Indirect taxes received by Public Admin.          | Standard version           | $GTE = GTET * TI$   |
|   | Fiscal policy rule version | $GTE = GV + GTR + GSUB + IS13V + GTRND - GTYPER - GTYC - GTYSOC - GTK - GTTI - GTRF - GTRK - TD2S - GBOR$ |
| Implicit rate of indirect taxation                | Standard version           | $RTI = RTITP * RTP$   |
|   | Fiscal policy rule version | $RTI = TI / CONSV$  |
| Total indirect taxes                              | Standard version           | $TI = RTI * CONSV$  |
|   | Fiscal policy rule version | $TI = GTE / GTETI$  |
| Public sector deficit                             | Standard version           | $GBOR = GV + GTR + GSUB + IS13V + GTRND - GTYPER - GTYC - GTYSOC - GTE - GTK - GTTI - GTRF - GTRK - TD2S$ |
|   | Fiscal policy rule version | $GBOR = (GDPMV * GBORR) / 100$  |
| Public sector deficit as % of GDP                 | Standard version           | $GBORR = 100 * GBOR / GDPMV$  |
| Implicit rate of taxes less subsidies on products | Fiscal policy rule version | $RTP = RTI / RTITP$   |

### Notes:

Exogenous variables are written in *italic*.

The econometrically estimated equations are highlighted in yellow. In this table they are presented in a very simplified form, only mentioning the explanatory variables with no reference to the functional form, lag structure or lagged dependent variables. An exact formulation is presented in Appendix 2.

The equations with coefficients derived from input-output matrices are highlighted in blue.

There are two versions in the model, concerning the Public Finance block, which affect five equations: the *standard version* and the *fiscal policy rule version*. In the *fiscal policy rule version* public deficit as % of GDP (GBORR) is exogenous and the adjustment is made through the rate of taxation (less subsidies) on products (RTP). Therefore GBORR is endogenous in the *standard version* and exogenous in the *fiscal policy rule version*, the opposite occurring with RTP (exogenous in the *standard version* and exogenous in the *policy rule version*).



## APPENDIX 2

### HERPOR 3

#### Econometrically estimated equations

#### 1. Sectors of activity

##### 1.1. Tradable sector (T)

##### 1.1.1. Actual Output (OT): (ECM estimated in two steps)

###### Long-run relationship:

$$\log(\text{OT}^*) = 2.65 - 0.64 \cdot \log(\text{ULCT}/\text{POT}) + 0.79 \cdot \log(\text{FDOT}) - 0.19 \cdot \log(\text{POT}/\text{PWORLD}) + 0.06 \cdot \log(\text{OW}) - 0.006 \cdot \text{T}$$

(3.47) (-10.2) (9.08) (-3.07) (0.80) (-1.40)

Estimation period: 1977-2006;  $R^2=0.99$  DW=0.97 ADF on residuals = -5.18\*\*

###### Short-run relationship:

$$\begin{aligned} \text{dlog}(\text{OT}) = & -0.006 - 0.71 \cdot [\log(\text{OT}) - \log(\text{OT}^*)]_{-1} + 0.76 \cdot \text{dlog}(\text{FDOT}) \\ & (-1.60) \quad (-3.96) \quad (7.81) \\ & - 0.45 \cdot \text{dlog}(\text{ULCT}/\text{POT}) - 0.18 \cdot \text{dlog}(\text{POT}/\text{PWORLD}) + 0.25 \cdot \text{dlog}(\text{OT})_{-1} \\ & (-5.93) \quad (-2.38) \quad (2.13) \end{aligned}$$

Estimation period: 1979-2006;  $R^2=0.78$  DW=1.63 BG1(p value) = 0.34

##### 1.1.2. Potential Output (OTPOT): (restricted least squares)

$$\log(\text{OTPOT}) = 0.079 + 0.35 \cdot \log(\text{KT}_{-1}) + 0.65 \cdot \log(\text{LT}) + 0.78 \cdot \log(\text{KTRAIN})$$

(1.68) (31.72)

Estimation period: 1977-2007;  $R^2=0.95$  DW=0.49 ADF on residuals (GAPOT) = -4.73\*

##### 1.1.3. Fixed investment (IT) (ECM estimated in two steps):

###### Long-run relationship:

$$\log(\text{IT}^*) = 3.91 + 0.42 \cdot \log(\text{OT}) - 0.21 \cdot \log[\text{PKT}^*(1-\text{CSFT})]$$

(1.83) (1.95) (-3.43)

Estimation period: 1978-2006;  $R^2=0.27$  DW=0.69 ADF on residuals = -4.58\*

###### Short-run relationship:

$$\text{dlog}(\text{IT}) = 0.003 - 0.54 \cdot [\log(\text{IT}) - \log(\text{IT}^*)]_{-1} + 0.42 \cdot \text{dlog}(\text{IT})_{-1} + 0.85 \cdot \text{GAPOT}_{-1}$$

(0.15) (-3.53) (2.44) (1.19)

Estimation period: 1979-2006;  $R^2=0.60$  DW=2.05 BG1(p value) = 0.51

##### 1.1.4. Output deflator (POT): (ECM estimated in one step)

$$\begin{aligned} \text{dlog}(\text{POT}) = & 0.13 + 0.63 \cdot \text{dlog}(\text{PWORLD})_{-1} + 0.68 \cdot \text{dlog}(\text{ULCT})_{-1} \\ & (2.23) \quad (4.05) \quad (3.46) \\ & - 0.49 \cdot \log(\text{POT})_{-1} + 0.23 \cdot \log(\text{PWORLD})_{-2} + 0.30 \cdot \log(\text{ULCT})_{-2} \\ & (-2.39) \quad (2.08) \quad (2.17) \end{aligned}$$

Estimation period: 1979-2007;  $R^2=0.95$  DW=1.66 BG1(p value) = 0.27

###### Implicit long-run relationship:

$$\log(\text{POT}^*) = 0.46 \cdot \log(\text{PWORLD})_{-1} + 0.61 \cdot \log(\text{ULCT})_{-1}$$

### 1.1.5. Employment (LT):

$$d\log(LT) = -0.013 + 0.49*d\log(OT) - 0.14*d\log(WT / POT) + 0.23*GAPOT_{-1}$$

(-6.19)      (7.32)                      (-1.83)                      (4.81)

Estimation period: 1978-2006; R<sup>2</sup>=0.74    DW=2.62

### 1.1.6. Wage rate (WT):

$$d\log(WT/POT/LPRT) = 0.076 - 0.013*UR + 0.33*d\log(WT/POT/LPRT)_{-1} - 0.67*d\log(WT/POT/LPRT)_{-2}$$

(2.82)      (-2.75)                      (2.12)                      (-4.46)

Estimation period: 1980-2006; R<sup>2</sup>=0.60    DW=1.94    BG1(p value) = 0.99

**Implicit long-run unemployment rate:** UR\* = 5,9%

## 1.2. Non-tradable sector (N)

### 1.2.1. Actual Output (ON): (ECM estimated in one step)

$$d\log(ON) = 1.24 + 0.71*d\log(FDON) - 0.45*\log(ON)_{-1} + 0.34*\log(FDON)_{-1} + 0.07*\log(OW)_{-1}$$

(1.74)      (10.35)                      (-3.32)                      (3.34)                      (1.80)

Estimation period: 1978-2006; R<sup>2</sup>=0.78    DW=2.14    BG1(p value) = 0.57

#### Implicit long-run relationship:

$$\log(ON^*) = 0.76*\log(FDON) + 0.15*\log(OW)$$

### 1.2.2. Fixed investment excluding housing and infrastructures (IN2):

(ECM estimated in one step)

$$d(IN2) = 4307 - 177.7*d(UR) + 0.28*d(ON) - 8795*d(PIN2/PON) - 4544*d(RIRLT)$$

(1.71)      (-1.33)                      (2.93)                      (-3.19)                      (-1.74)

$$0.63*d(TRIN/PIN2) - 4715*(PIN2/PON)_{-1} - 0.63*IN2_{-1} + 0.12*(ON)_{-1}$$

(0.82)                      (-2.86)                      (-3.53)                      (2.66)

Estimation period: 1978-2006; R<sup>2</sup>=0.75    DW=2.30    BG1(p value) = 0.25

#### Implicit long-run relationship:

$$IN2^* = -7465*(PIN2/PON) + 0.19*ON$$

### 1.2.3. Output deflator (PON): (ECM estimated in one step)

$$d\log(PON) = 0.186 + 0.30*d\log(PWORLD) + 0.35*d\log(ULCN) - 0.45*\log(PON)_{-1}$$

(2.45)      (5.55)                      (5.58)                      (-2.55)

$$+ 0.17*\log(PWORLD)_{-1} + 0.30*\log(ULCN)_{-1}$$

(2.76)                      (2.18)

Estimation period: 1978-2006; R<sup>2</sup>=0.97    DW=1.90    BG1(p value) = 0.91

#### Implicit long-run relationship:

$$\log(PON^*) = 0.39*\log(PWORLD) + 0.66*\log(ULCN)$$

### 1.2.4. Employment (LLN):

$$\text{dlog(LLN)} = 0.004 + 0.46 * \text{dlog(ON)} - 0.12 * \text{dlog(ULCN/PON)}_{-1} + 0.40 * \text{GAPGDP}_{-1}$$

(1.16)    (4.58)                      (-1.70)                                      (5.56)

Estimation period: 1979-2006; R<sup>2</sup>=0.68    DW=1.67

### 1.2.5. Wage rate (WN): (ECM estimated in two steps)

#### Long-run relationship:

$$\log(\text{WN}^*) = -0.003 + 1.03 * \log(\text{WT}) + 0.31 * \log(\text{LPRN/LPRT})$$

(-0.08)    (108.9)                      (4.42)

Estimation period: 1977-2006; R<sup>2</sup>=0.99    DW=0.85    ADF on residuals = -3.95\*

#### Short-run relationship:

$$\text{dlog(WN)} = -0.001 - 0.44 * [\log(\text{WN}) - \log(\text{WN}^*)]_{-1} + 0.86 * \text{dlog(WT)} + 0.23 * \text{dlog(LPRN/LPRT)}$$

(-0.30)    (-3.40)                                      (12.76)                      (2.42)

$$+ 0.16 * \text{dlog(WN)}_{-1}$$

(2.26)

Estimation period: 1979-2006; R<sup>2</sup>=0.98    DW=1.70    BG1(p value) = 0.44

## 1.3. Agricultural sector (A)

### 1.3.1. Wage rate (WA): (ECM estimated in one step)

$$\text{dlog(WA)} = -0.07 + 1.08 * \text{dlog(WT)} - 0.42 * \log(\text{WA})_{-1} + 0.38 * \log(\text{WT})_{-1}$$

(-0.90)    (3.10)                      (-3.56)                      (3.24)

Estimation period: 1978-2006; R<sup>2</sup>=0.79    DW=1.78    BG1(p value) = 0.22

#### Implicit long-run relationship:

$$\log(\text{WA}^*) = 0.9 * \log(\text{WT})$$

## 1.4. Non-market services sector (G)

### 1.4.1. Wage rate (WG): (ECM estimated in one step)

$$\text{dlog(WG)} = 0.27 + 0.64 * \text{dlog(WT)} - 0.33 * \log(\text{WG/WT})_{-1} - 0.0027 * \text{GBORR}_{-1} - 0.01 * \text{UR}_{-1}$$

(8.79)    (6.20)                      (-7.26)                      (-1.47)                      (-2.86)

Estimation period: 1978-2006; R<sup>2</sup>=0.94    DW=2.30    BG1(p value) = 0.40

#### Implicit long-run relationship:

$$\log(\text{WG}) = \log(\text{WT}) + \text{constant} - 0.008 * \text{GBORR} - 0.027 * \text{UR}$$

## 2. Global economy

### 2.1. Potential output (YPOT): (restricted least squares)

$$\log(\text{YPOT}) = 0.29 + 0.17 * \log(\text{KPR})_{-2} + 0.06 * \log(\text{KINF})_{-2} + 0.77 * \log(\text{L}) + 1.30 * \log(\text{KTRAIN})_{-1} - 0.01 * \text{T} * \log(\text{KTRAIN})_{-1}$$

(1.76)                                      (10.64)                                      (-5.97)

Estimation period: 1977-2006; R<sup>2</sup>=0.99    DW=0.38    ADF on residuals (GAPGDP) = -3.35\*

## 2.2. Private consumption (CONS): (ECM estimated in one step)

$$\begin{aligned} \text{dlog(CONS)} = & 2.24 - 0.50 \cdot \text{log(CONS)}_{-1} - 0.0029 \cdot \text{IRD}_{-1} - 0.005 \cdot \text{UR}_{-1} + 0.30 \cdot \text{log(YRPERD-BTPRNE/PCONS)}_{-1} \\ & (2.25) \quad (-3.43) \quad (-3.70) \quad (-1.81) \quad (2.62) \\ & + 0.37 \cdot \text{dlog(YRPERD-BTPRNE/PCONS)} - 0.01 \cdot \text{d(UR)} - 0.003 \cdot \text{d(IRD)} + 0.005 \cdot \text{T} + 0.16 \cdot \text{dlog(CONS)}_{-1} \\ & (3.43) \quad (-3.19) \quad (-4.24) \quad (1.91) \quad (1.87) \end{aligned}$$

Estimation period: 1977-2006;  $R^2=0.90$  DW=2.24

### Implicit long-run relationship:

$$\text{log(CONS}^*) = \text{constant} + 0.59 \cdot \text{log(YRPERD-BTPRNE/PCONS)} - 0.006 \cdot \text{IRD} - 0.009 \cdot \text{UR} + 0.009 \cdot \text{T}$$

## 2.3. Housing investment (IH): (ECM estimated in one step)

$$\begin{aligned} \text{dlog(IH)} = & 5.19 - 0.58 \cdot \text{log(IH)}_{-1} - 0.01 \cdot \text{IRLT}_{-1} + 0.50 \cdot \text{dlog(YRPERD)} - 0.008 \cdot \text{d(IRLT)} - 0.21 \cdot \text{d2003IH} \\ & (7.55) \quad (-7.55) \quad (-6.95) \quad (2.10) \quad (-5.27) \quad (-8.87) \end{aligned}$$

Estimation period: 1977-2006;  $R^2=0.84$  DW= 1.57 BG1(p value) = 0.43

### Implicit long-run relationship:

$$\text{log(IH}^*) = \text{constant} - 0.02 \cdot \text{IRLT} - 0.36 \cdot \text{d2003IH}$$

## 2.4. Private Consumption Deflator (PCONS): (ECM estimated in one step)

$$\begin{aligned} \text{dlog(PCONS)} = & 0.0006 + 0.16 \cdot \text{dlog(PM)} + 0.92 \cdot \text{dlog(PGDPM)} - 0.41 \cdot \text{log(PCONS)}_{-1} \\ & (0.24) \quad (5.37) \quad (15.00) \quad (-4.14) \\ & + 0.05 \cdot \text{log(PM)}_{-1} + 0.37 \cdot \text{log(PGDPM)}_{-1} \\ & (2.93) \quad (4.12) \end{aligned}$$

Estimation period: 1959-2006;  $R^2=0.98$  DW= 2.10 BG1(p value) = 0.61

### Implicit long-run relationship:

$$\text{log(PCONS}^*) = 0.13 \cdot \text{log(PM)} + 0.89 \cdot \text{log(PGDPM)}$$

## 2.5. Equipment deflator (PIME): (ECM estimated in one step)

$$\begin{aligned} \text{dlog(PIME)} = & 0.008 + 0.36 \cdot \text{dlog(PM)} - 0.34 \cdot \text{log(PIME)}_{-1} + 0.06 \cdot \text{log(POT)}_{-1} + 0.25 \cdot \text{log(PM)}_{-1} \\ & (2.35) \quad (3.86) \quad (-3.86) \quad (1.25) \quad (4.30) \end{aligned}$$

Estimation period: 1978-2006;  $R^2=0.97$  DW= 1.43 BG1(p value) = 0.19

### Implicit long-run relationship:

$$\text{log(PIME}^*) = 0.73 \cdot \text{log(PM)} + 0.17 \cdot \text{log(POT)}$$

## 2.6. Construction deflator (PIC): (ECM estimated in one step)

$$\begin{aligned} \text{dlog(PIC)} = & -0.13 + 0.14 \cdot \text{dlog(PM)} + 0.35 \cdot \text{dlog(WN)} - 0.39 \cdot \text{log(PIC)}_{-1} + 0.22 \cdot \text{log(PM)}_{-1} \\ & (-3.18) \quad (1.82) \quad (2.71) \quad (-5.43) \quad (5.00) \\ & + 0.08 \cdot \text{log(ULCN)}_{-1} + 0.008 \cdot \text{T} \\ & (1.61) \quad (6.83) \end{aligned}$$

Estimation period: 1978-2006;  $R^2 = 0.97$  DW = 1.98 BG1(p value) = 0.97

**Implicit long-run relationship:**

$$\log(\text{PIC}^*) = 0.56 \cdot \log(\text{PM}) + 0.21 \cdot \log(\text{ULCN}) + 0.021 \cdot T$$

**2.7. Labour Force (LF):** (ECM estimated in one step)

$$\text{dlog(LF)} = 0.021 + 0.75 \cdot \text{dlog(L)} - 0.29 \cdot \log(\text{LF/L})_{-1} - 0.50 \cdot \text{dlog(L)}_{-1} + 0.33 \cdot \text{dlog(LF)}_{-1}$$

(5.28)      (9.52)                      (-4.62)                      (-5.26)                      (2.73)

Estimation period: 1977-2006;  $R^2 = 0.84$      $DW = 2.31$      $BG1(p \text{ value}) = 0.24$

**Implicit long-run relationship:** (constant long-run unemployment rate)

$$\log(\text{LF}^*) = \text{constant} + \log(L)$$

**NOTES:**

For any variable X,

$$\text{dlog}(X) = \log(X) - \log(X(-1))$$

$$d(X) = X - X(-1)$$

$X^*$  represents the long-run equilibrium value of X.

Exogenous variables are in bold.

t ratios are presented in brackets below the corresponding estimated parameters.

For the estimated long-run relationships cointegration was tested using the Engle-Granger ADF test on the residuals (Engle and Granger, 1987). One star in this test means that the null hypothesis of no cointegration is rejected at a 10% level of significance while two stars means the rejection at 5%, using the MacKinnon (1991) critical values.

In the regressions that included the lagged dependent variable in the regressors, an additional test for serial correlation was performed since the DW test is not valid in this case. This test, presented as BG1, is the Breush-Godfrey chi-square test for the null hypothesis of uncorrelated residuals against the alternatives of AR(1) or MA(1) (*vide* Johnston, 1984, pp 319-321). A high p value (more than 0.10) leads to accepting the null hypothesis (absence of first order autocorrelation in the residuals).

## APPENDIX 3 – THE HERPOR VARIABLES

### 1. Endogenous variables

| Designation | Description   |
|-------------|---|
| CONS        | Private Consumption (at 2000 prices)  |
| CONSV       | Private Consumption (at current prices)   |
| CSFT        | Weight of investment aids on sector T investment                                    |
| DD          | Domestic Demand (at 2000 prices)  |
| DEPT        | Average depreciation rate on sector T capital stock                                 |
| DS          | Change in inventories+Net acquisition of valuables (at 2000 prices)                 |
| DSV         | Change in inventories+Net acquisition of valuables (at current prices)              |
| FDON        | Weighted Domestic Demand for sector N (using 2000 I-O coefficients, 2000 prices)    |
| FDOT        | Weighted Domestic Demand for sector T (using 2000 I-O coefficients, 2000 prices)    |
| G           | Public Consumption (at 2000 prices)   |
| GAPGDP      | Output gap (total economy)  |
| GAPOT       | Output gap (sector T)   |
| GBOR        | Public sector deficit (at current prices)   |
| GBORR       | GBOR as % of GDP  |
| GDPBP       | GDP at basic prices (at 2000 prices)  |
| GDPBPV      | GDP at basic prices (at current prices)   |
| GDPFCV      | GDP at factor costs (at current prices)   |
| GDPM        | GDP at market prices (at 2000 prices)   |
| GDPMV       | GDP at market prices (at current prices)  |
| GND         | Public debt   |
| GNPV        | Gross National Product (at current prices)  |
| GTE         | Indirect taxes received by Public Administration                                    |
| GTK         | Capital tax revenue   |
| GTRND       | Interests on Public debt  |
| GTTI        | Public sector Gross Operating Surplus+Investment income                             |
| GTY         | Public revenue from direct taxes and social contributions                           |
| GTYC        | Direct taxes on Corporations  |
| GTYPER      | Direct taxes on Households  |
| GTYSOC      | Social Contributions received by Public Administrations                             |
| GV          | Public Consumption (at current prices)  |
| I           | Total Gross Fixed Capital Formation (at 2000 prices)                                |
| IABC        | Investment in Construction excluding Housing - sector A (at 2000 prices)            |
| IAME        | Investment in Equipment - sector A (at 2000 prices)                                 |
| IAV         | Total fixed investment - sector A (at current prices)                               |
| IBC         | Total investment in construction, excluding housing (at 2000 prices)                |
| IC          | Total investment in construction, including housing (at 2000 prices)                |
| IG          | Fixed investment - sector G (at 2000 prices)  |
| IGBC        | Investment in Construction excluding Housing - sector G (at 2000 prices)            |
| IGME        | Investment in Equipment -sector G (at 2000 prices)                                  |
| IGV         | Total fixed investment - sector G (at current prices)                               |
| IH          | Housing investment (at 2000 prices)   |
| IHV         | Housing investment (at current prices)  |
| IINF        | Investment in infrastructures (at 2000 prices)                                      |
| IME         | Investment in Machinery and Equipment (at 2000 prices)                              |
| IN          | Total fixed investment - sector N, excluding housing (at 2000 prices)               |
| IN2         | Fixed investment - sector N, excluding housing and infrastructures (at 2000 prices) |



|         |  |
|---------|--|
| INBC    | Investment in Construction excluding Housing - sector N (at 2000 prices)                   |
| ININF   | Investment in infrastructures - sector N (at 2000 prices)                                  |
| INME    | Investment in equipment - sector N (at 2000 prices)  |
| INV     | Total fixed investment - sector N, excluding housing (at current prices)                   |
| IT      | Total fixed investment - sector T (at 2000 prices)   |
| ITBC    | Investment in Construction - sector T (at 2000 prices)                                     |
| ITME    | Investment in Equipment - sector T (at 2000 prices)  |
| ITV     | Total fixed investment -sector T (at current prices)                                       |
| IV      | Total Gross Fixed Capital Formation (at current prices)                                    |
| KA      | Capital stock in A sector (at 2000 prices)   |
| KABC    | Capital stock of construction - sector A (2000 prices)                                     |
| KAME    | Capital stock of equipment - sector A (2000 prices)  |
| KG      | Capital stock - sector G (2000 prices)   |
| KGBC    | Capital stock of non-residential construction - sector G (at 2000 prices)                  |
| KGME    | Capital stock of equipment - sector G (2000 prices)  |
| KINF    | Capital stock of infrastructures (at 2000 prices)  |
| KN      | Capital stock - sector N, excluding housing (at 2000 prices)                               |
| KNBC    | Capital stock of non-residential construction - sector N (at 2000 prices)                  |
| KNINF   | Capital stock of infrastructures - sector N (at 2000 prices)                               |
| KNME    | Capital stock of equipment - sector N (2000 prices)  |
| KPR     | Total capital stock, excluding infrastructures and Housing (at 2000 prices)                |
| KPTRAIN | Stock of professional training (average nº years of training for population aged 15 to 64) |
| KT      | Capital stock in the T sector (2000 prices)  |
| KTBC    | Capital stock of construction - sector T (2000 prices)                                     |
| KTME    | Capital stock of equipment - sector T (2000 prices)  |
| KTRAIN  | Total Human Capital (average nº years of education+training for population aged 15 to 64)  |
| L       | Total Employment (volume)  |
| LAEMP   | Employees - sector A (volume)  |
| LASEMP  | Self employment in the A sector (volume)   |
| LEMP    | Employees (all sectors - volume)   |
| LF      | Labour Force (thousands of individuals)  |
| LG      | Employment in the G sector (volume)  |
| LGEMP   | Employees in the G sector (volume)   |
| LGSEMP  | Self Employment in the G sector (volume)   |
| LLN     | Employment in the N sector (volume)  |
| LLNEMP  | Employees in the N sector (volume)   |
| LLNSEMP | Self employment in the N sector (volume)   |
| LPRN    | Labour productivity in the N sector (at 2000 prices)                                       |
| LPROD   | Total labour productivity (at 2000 prices)   |
| LPRT    | Labour productivity in the T sector (at 2000 prices)                                       |
| LT      | Employment in the T sector (volume)  |
| LTEMP   | Employees in the T sector (volume)   |
| LTSEMP  | Self employment in the T sector (volume)   |
| NTS     | External Balance of Goods and Services (at 2000 prices)                                    |
| NTSV    | External Balance of Goods and Services (at current prices)                                 |
| OAV     | Gross Value Added at basic prices in the A sector (at current prices)                      |
| OG      | Gross Value Added at basic prices in the G sector (at 2000 prices)                         |
| OGV     | Gross Value Added at basic prices in the G sector (at current prices)                      |
| ON      | Gross Value Added at basic prices in the N sector (at 2000 prices)                         |
| ONV     | Gross Value Added at basic prices in the N sector (at current prices)                      |
| OT      | Gross Value Added at basic prices in the T sector (at 2000 prices)                         |

|        |  |
|--------|--|
| OTPOT  | Potential Output in the T sector (at 2000 prices)                      |
| OTV    | Gross Value Added at basic prices in the T sector (at current prices)  |
| PCONS  | Private consumption deflator (index, 2000=1)                           |
| PG     | Public consumption deflator (index, 2000=1)                            |
| PGDPBP | GDP deflator, at basic prices (index, 2000=1)                          |
| PGDPM  | GDP deflator, at market prices (index, 2000=1)                         |
| PI     | deflator of total investment (index, 2000=1)                           |
| PIA    | deflator of sector A investment (index, 2000=1)                        |
| PIC    | Deflator of Construction Investment (including Housing)                |
| PIG    | Deflator of sector G Investment  |
| PIME   | Deflator of Equipment Investment                                       |
| PIN    | Deflator of sector N investment (excluding housing)                    |
| PIN2   | Deflator of sector N investment, excluding housing and infrastructures |
| PIT    | Deflator of sector T investment  |
| PKT    | User cost of capital in the T sector                                   |
| POG    | Deflator of OGV  |
| PON    | Deflator of ONV  |
| POT    | Deflator of OTV  |
| PTP    | Deflator of taxes less subsidies on products                           |
| RDEBT  | Public debt as a % of GDP  |
| RIRLT  | Real interest rate on 3 to 5 year loans                                |
| RTI    | Implicit rate of Indirect taxation (weight on Private Consumption)     |
| RULCT  | Real unit labour costs in the T sector (at 2000 prices)                |
| SAV    | Household gross savings (at current prices)                            |
| SUB    | Total Subsidies (at current prices)                                    |
| TI     | Total Indirect taxes   |
| TP     | Taxes less subsidies on products                                       |
| U      | Unemployment   |
| ULC    | Total Unit labour costs  |
| ULCN   | unit labour costs in the N sector (at current prices)                  |
| ULCT   | unit labour costs in the T sector (at current prices)                  |
| UR     | unemployment rate  |
| URBAR  | Two-year average of UR   |
| W      | Average annual wage rate (including employers' contributions)          |
| WA     | Annual wage rate in the A sector                                       |
| WG     | Annual wage rate in the G sector                                       |
| WN     | Annual wage rate in the N sector                                       |
| WR     | Annual average real wage rate in the T+N sectors                       |
| WT     | Annual wage rate in the T sector                                       |
| YC     | Proxy of total profits (at current prices)                             |
| YCA    | Proxy of profits in the A sector (at current prices)                   |
| YCN    | Proxy of profits in the N sector (at current prices)                   |
| YCT    | Proxy of profits in the T sector (at current prices)                   |
| YPER   | Personal income before tax (at current prices)                         |
| YPERD  | Personal disposable income (at current prices)                         |
| YPOT   | Potential output (at 2000 prices)                                      |
| YRPERD | Real personal disposable income (at 2000 prices)                       |
| YW     | Compensation of employees (at current prices)                          |
| YWA    | Compensation of employees (at current prices) in the A sector          |
| YWN    | Compensation of employees (at current prices) in the N sector          |
| YWT    | Compensation of employees (at current prices) in the T sector          |

## 2. Exogenous variables

| Designation | Description   |
|-------------|---|
| ADPTP       | Adjustment factor for PTP   |
| ADS         | Proportion of DS in the output of sectors A+T+N (at 2000 prices)  |
| BPTRNE      | Net private international transfers (at current prices)   |
| D2003IH     | Dummy which assumes the value 1 after 2002  |
| DAT         | Exogenous component of Public Debt change   |
| DEPBC       | Depreciation rate for Construction excluding housing  |
| DEPME       | Depreciation rate for Equipment   |
| DEPTRAIN    | Depreciation rate for the stock of professional training  |
| ECSUB       | Subsidies paid by EU  |
| GENW        | Diff. between Public Consumption and Compensation of Employees in the G sector (at current prices)      |
| GSUB        | Subsidies paid by Public Administration (at current prices)   |
| GTETI       | Proportion of indirect taxes received by Public Administration  |
| GTR         | Social benefits and other current transfers between Public Admin. and other domestic agents (net)       |
| GTRF        | Net current transfers between Public Administration and the rest of the World (received less paid)      |
| GTRK        | Net capital transfers between Public Administration and all other agents, incl. EU (received less paid) |
| IA          | Total fixed investment in the A sector (at 2000 prices)   |
| IGVO        | Difference between total investment in the G sector and Public Investment (at current prices)           |
| ININFV      | Investment in infrastructures - sector N (at current prices)  |
| IRD         | Nominal Interest rate on deposits from 181 days to 1 year   |
| IRLT        | Nominal interest rate on 3 to 5 year loans  |
| IS13V       | Public investment (GFCF) at current prices  |
| KEDU        | Stock of Education (average nº years of education for population aged 15 to 64)                         |
| LA          | Employment in the A sector (volume) (thousands)   |
| N1564       | Population aged 15 to 64 (thousands of individuals)   |
| AO          | Gross Value Added at basic prices in the A sector (at 2000 prices)                                      |
| OGVO        | Proxy of corporate gross profits in sector G (at current prices)  |
| OW          | International Demand (volume index, 2000=1)   |
| PDS         | Deflator of DSV   |
| PM          | Deflator of Imports   |
| PMIE        | International trade price index, converted to national currency (2000=1)                                |
| POA         | Deflator of OAV   |
| POGW        | Ratio between the output deflator and the wage rate in the G sector                                     |
| Ptrain      | Investment in Professional training (thousands of person-year of training)                              |
| PWORLD      | Price index of world manufacturing output, converted to national currency (2000=1)                      |
| RCS         | Proxy of corporate gross saving rate (weight on GDP at factor cost)                                     |
| RGDI        | Interest rate implicit on public debt   |
| RGTK        | Implicit rate of capital tax (weight on GDP)  |
| RGTTI       | Weight of GTTI on GDP   |
| RGTYC       | Implicit rate of direct corporate taxation  |
| RGTYPER     | Implicit rate of direct household taxation  |
| RGTYSOC     | Implicit rate of social contributions received by Public Administrations                                |



|         |   |
|---------|---|
| RPGO    | Ratio between Public Consumption deflator and the output deflator of the G sector |
| RTITP   | Ratio between total indirect taxes and taxes less subsidies on products           |
| RTP     | Implicit rate of taxes less subsidies on products (weight on private consumption) |
| SEARAT  | Fraction of self employed in LA   |
| SEN RAT | Fraction of self employed in LLN  |
| SETRAT  | Fraction of self employed in LT   |
| T       | Time index: 1977 =1   |
| TD2S    | Net Direct taxes on Households (received less paid) from abroad (value)           |
| TRIN    | Public aids to Investment in the N sector   |
| TRIT    | Public aids to Investment in the T sector   |
| VFPF    | Change in household net participation on Pension funds                            |
| WIAME   | Fraction of IA consisting of Machinery and equipment                              |
| WIGME   | Fraction of IG consisting of Machinery and equipment                              |
| WINME   | Fraction of IN consisting of Machinery and equipment                              |
| WITME   | Fraction of IT consisting of Machinery and equipment                              |
| YFN     | Net factor income (received less paid) from abroad (value)                        |
| YGSEMP  | Self employed income in the G sector (value)                                      |
| YWG     | Compensation of Employees in the G sector (at current prices)                     |

## APPENDIX 4 – HERPOR SECTORS

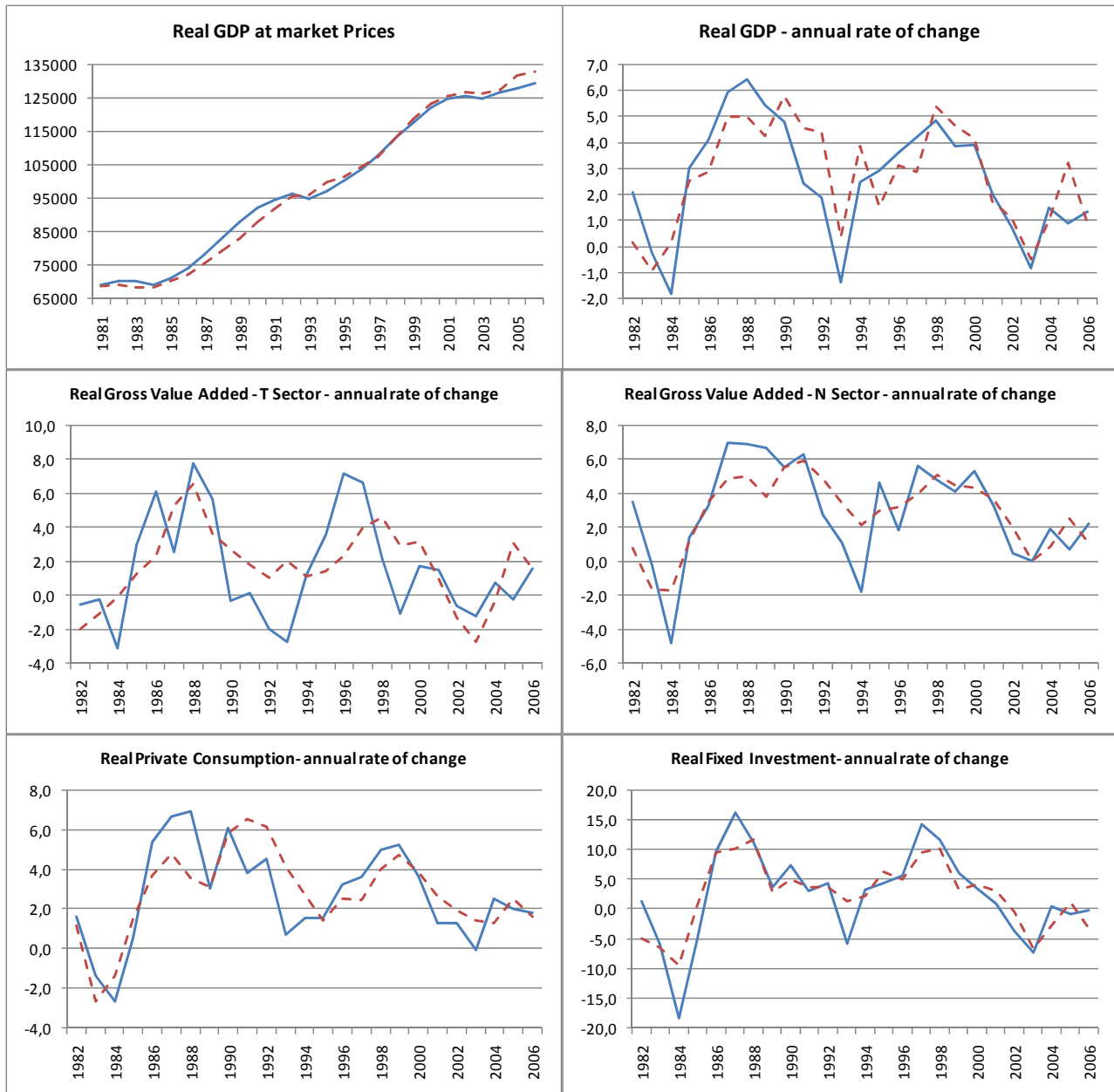
| Description   | ESA 95<br>(A60) |
|---|-----------------|
| <b>SECTOR A</b>   |                 |
| Agriculture, hunting and related service activities   | 1               |
| Forestry, logging and related service activities  | 2               |
| Fishing, aquaculture and service activities incidental to fishing   | 5               |
| <b>SECTOR T (TRADABLE)</b>  |                 |
| Mining of coal and lignite; extraction of peat  | 10              |
| Extraction of crude petroleum and natural gas; service activities incidental to oil and gas extraction, excluding surveying     | 11              |
| Mining of uranium and thorium ores  | 12              |
| Mining of metal ores  | 13              |
| Other mining and quarrying  | 14              |
| Manufacture of food products and beverages  | 15              |
| Manufacture of tobacco products   | 16              |
| Manufacture of textiles   | 17              |
| Manufacture of wearing apparel; dressing and dyeing of fur  | 18              |
| Tanning and dressing of leather; manufacture of luggage, handbags, saddlery, harness and footwear                               | 19              |
| Manufacture of wood and of products of wood and cork, except furniture; manufacture of articles of straw and plaiting materials | 20              |
| Manufacture of paper and paper products   | 21              |
| Publishing, printing and reproduction of recorded media   | 22              |
| Manufacture of coke, refined petroleum products and nuclear fuel  | 23              |
| Manufacture of chemicals and chemical products  | 24              |
| Manufacture of rubber and plastics products   | 25              |
| Manufacture of other non-metallic mineral products  | 26              |
| Manufacture of basic metals   | 27              |
| Manufacture of fabricated metal products, except machinery and equipment  | 28              |
| Manufacture of machinery and equipment n.e.c.   | 29              |
| Manufacture of office, accounting and computing machinery   | 30              |
| Manufacture of electrical machinery and apparatus n.e.c.  | 31              |
| Manufacture of radio, television and communication equipment and apparatus  | 32              |
| Manufacture of medical, precision and optical instruments, watches and clocks   | 33              |
| Manufacture of motor vehicles, trailers and semi-trailers   | 34              |
| Manufacture of other transport equipment  | 35              |
| Manufacture of furniture; manufacturing n.e.c.  | 36              |
| Water transport   | 61              |
| Air transport   | 62              |

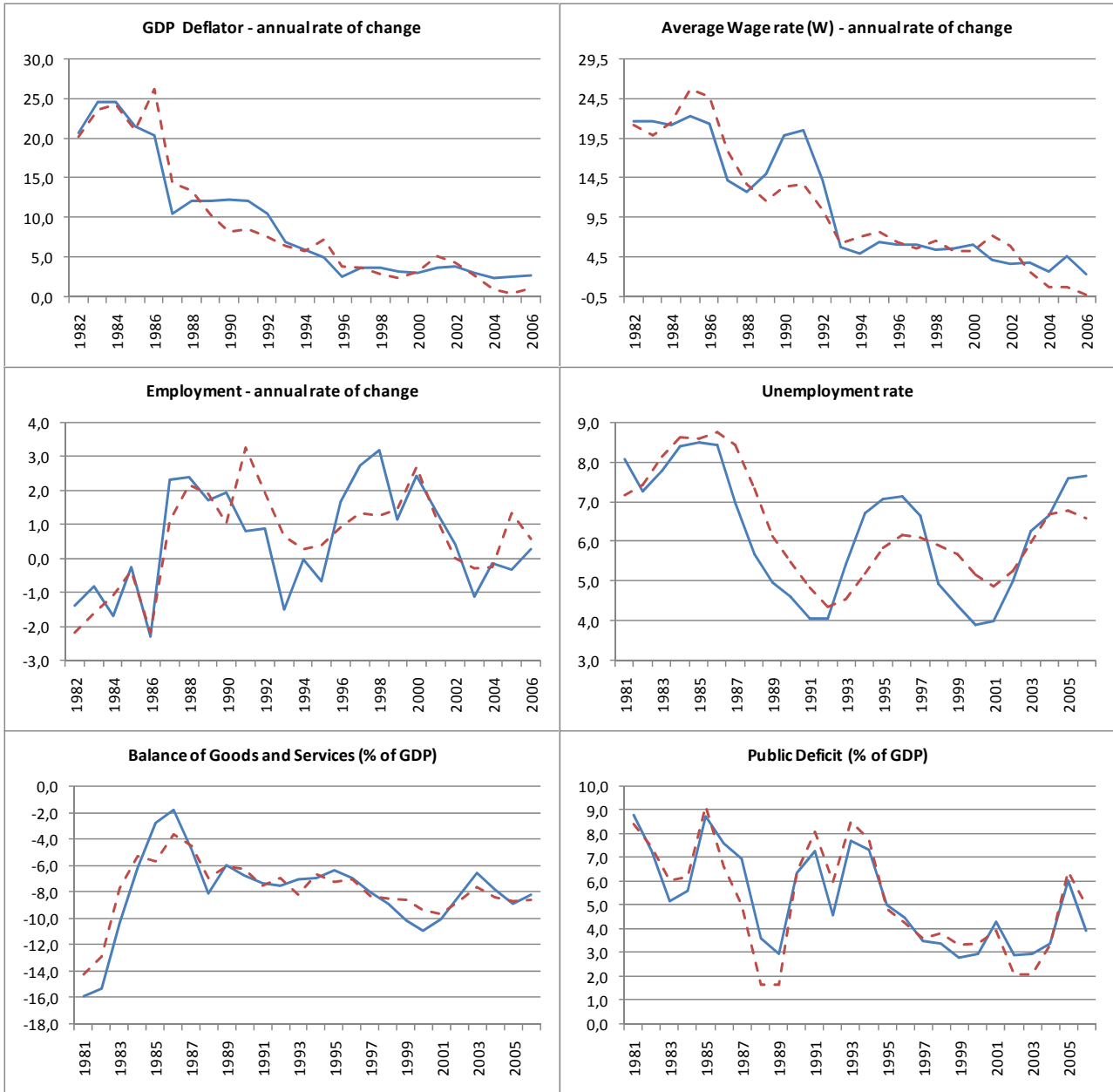
| <b>SECTOR N (PREDOMINANTLY NON TRADABLE)</b>   |    |
|--|----|
| Recycling  | 37 |
| Electricity, gas, steam and hot water supply   | 40 |
| Collection, purification and distribution of water   | 41 |
| Construction   | 45 |
| Sale, maintenance and repair of motor vehicles and motorcycles; retail sale of automotive fuel                 | 50 |
| Wholesale trade and commission trade, except of motor vehicles and motorcycles                                 | 51 |
| Retail trade, except of motor vehicles and motorcycles; repair of personal and household goods                 | 52 |
| Hotels and restaurants   | 55 |
| Land transport; transport via pipelines  | 60 |
| Supporting and auxiliary transport activities; activities of travel agencies                                   | 63 |
| Post and telecommunications  | 64 |
| Financial intermediation, except insurance and pension funding   | 65 |
| Insurance and pension funding, except compulsory social security   | 66 |
| Activities auxiliary to financial intermediation   | 67 |
| Real estate activities   | 70 |
| Renting of machinery and equipment without operator and of personal and household goods                        | 71 |
| Computer and related activities  | 72 |
| Other business activities  | 74 |
| Activities of membership organizations n.e.c.  | 91 |
| Recreational, cultural and sporting activities   | 92 |
| Other service activities   | 93 |
| Activities of private households as employers and undifferentiated production activities of private households | 95 |
| <b>SECTOR G (PREDOMINANTLY NON MARKET SERVICES)</b>  |    |
| Research and development   | 73 |
| Public administration and defence; compulsory social security  | 75 |
| Education  | 80 |
| Health and social work   | 85 |
| Sewage and refuse disposal, sanitation and similar activities  | 90 |

## APPENDIX 5 – HERPOR 3 – HISTORICAL DYNAMIC SIMULATION (1981-2006)

### Comparison of actual and simulation values for selected key variables

(----- Actual    - - - - Simulated)



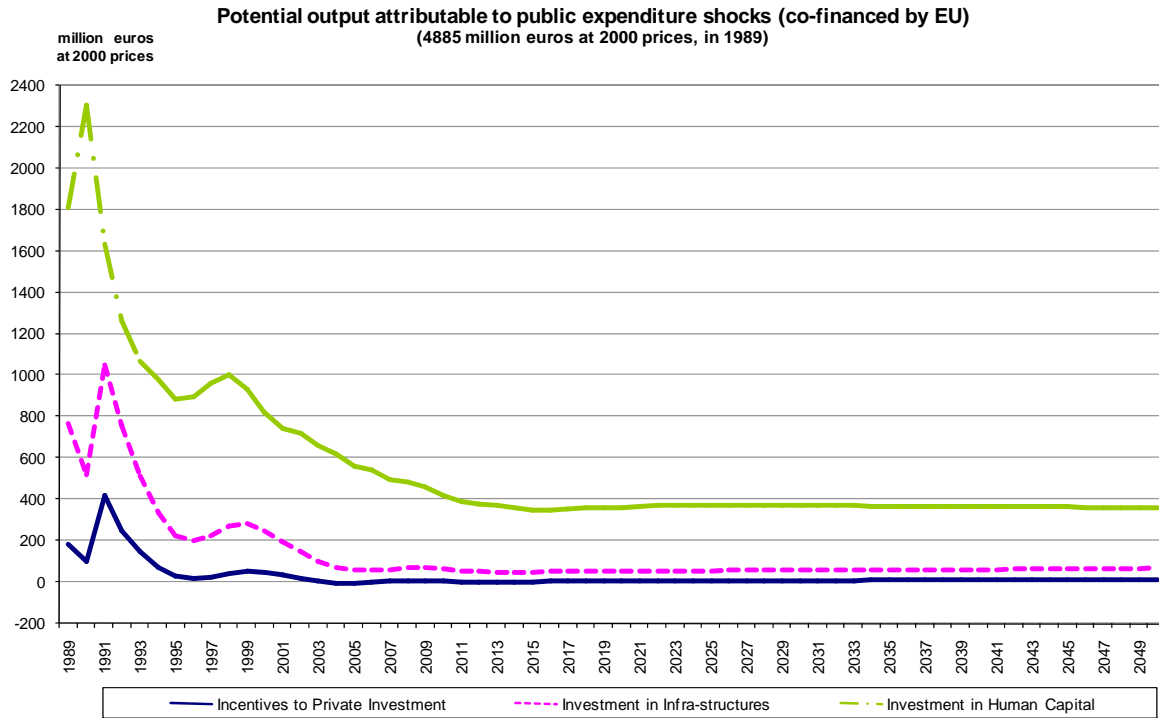




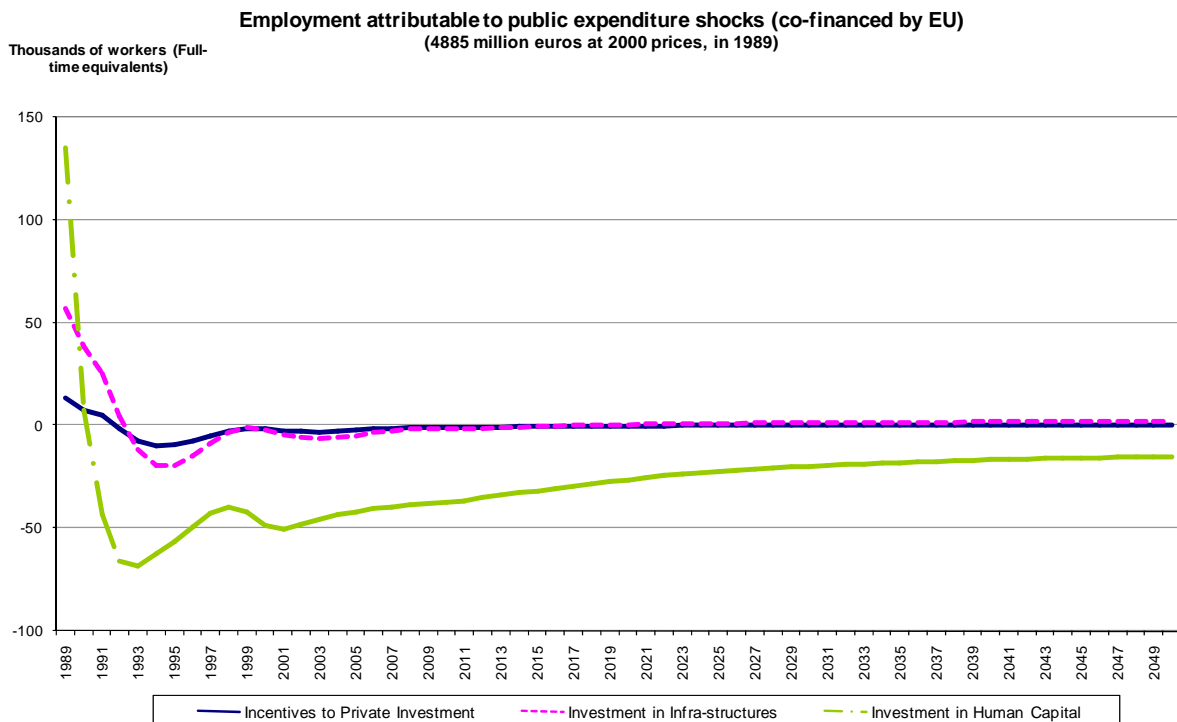
APPENDIX 6

**IMPACT OF DIFFERENT TYPES OF PUBLIC EXPENDITURE (CO-FINANCED BY EU FUNDS)**  
**(public expenditure shock of 4885 million euros at 2000 prices, in 1989)**

Graph A6-1

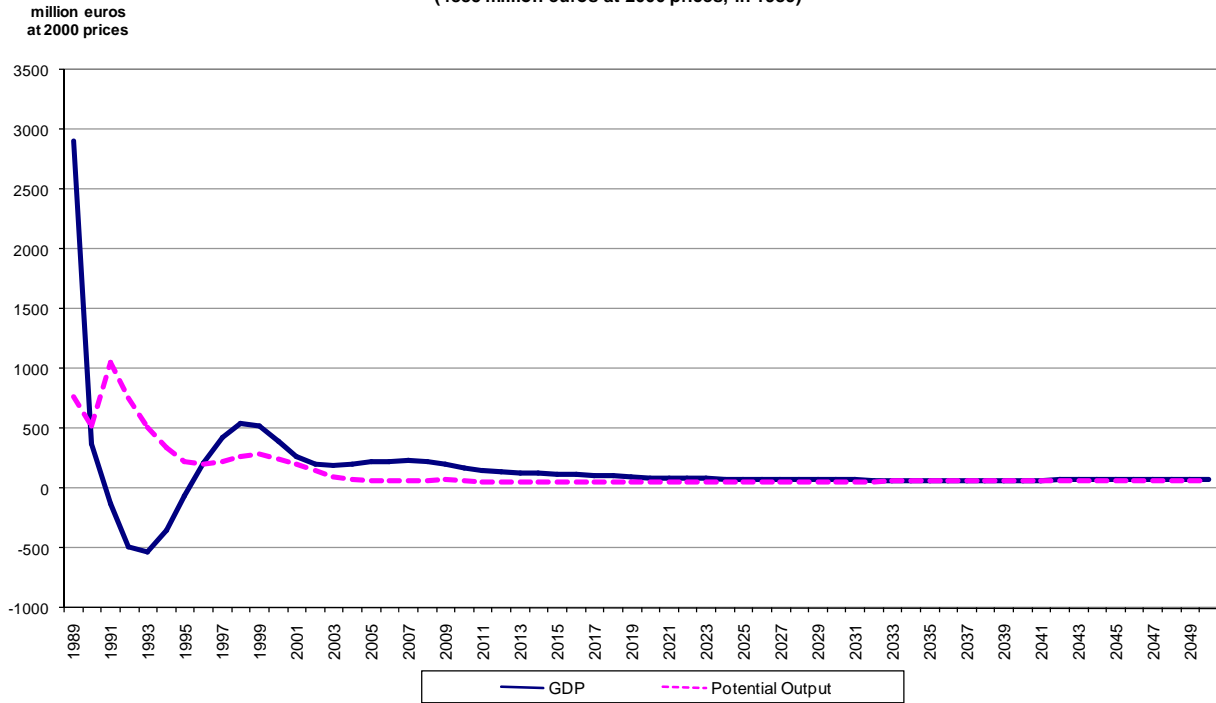


Graph A6-2



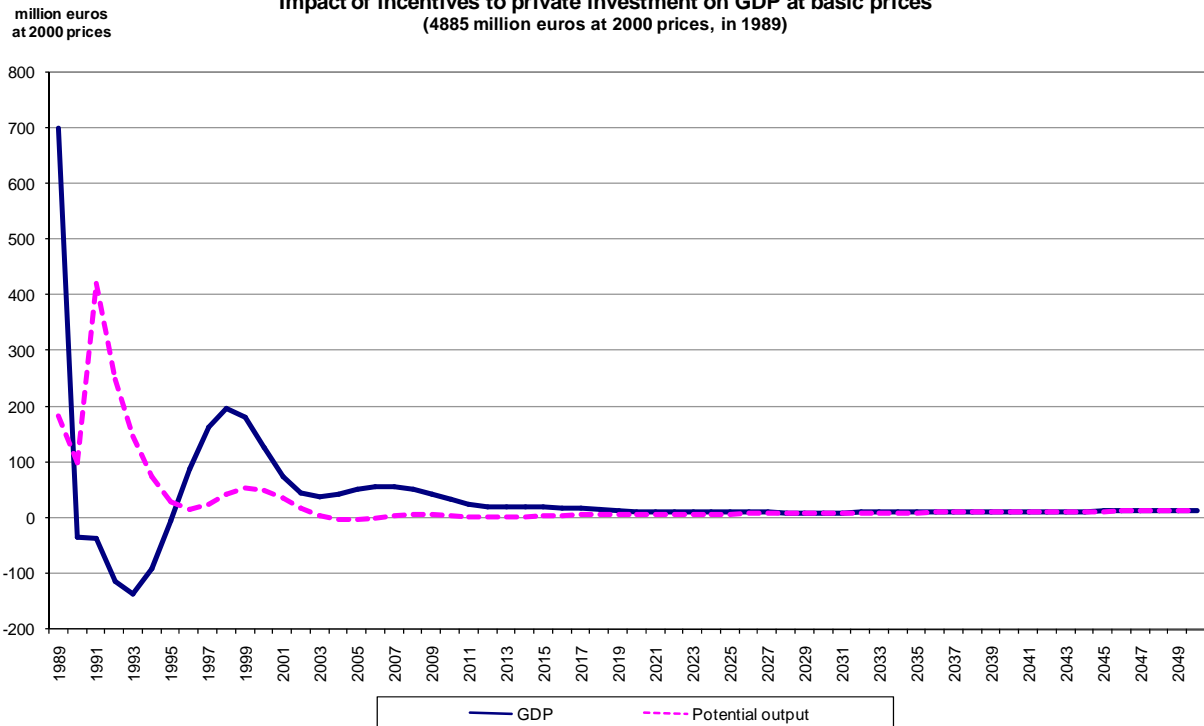
**Graph A6-3**

**Impact of investment in infra-structures on GDP at basic prices**  
(4885 million euros at 2000 prices, in 1989)



**Graph A6-4**

**Impact of incentives to private investment on GDP at basic prices**  
(4885 million euros at 2000 prices, in 1989)



Graph A6-5

Impact of Investment in Human Capital on GDP at basic prices  
(4885 million euros at 2000 prices, in 1989)

